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Reputation Spillover Across Relationships: Reviving Reputation Models of Debt

Harold L. Cole

Federal Reserve Bank of Minneapolis

Patrick J. Kehoe

University of Pennsylvania and
Federal Reserve Bank of Minneapolis

ABSTRACT

A traditional explanation for why sovereign governments repay debts is that they want to keep good reputations so they can easily borrow more. Bulow and Rogoff show that this argument is invalid under two conditions: (i) there is a single debt relationship, and (ii) regardless of their past actions, governments can earn the (possibly state-contingent) market rate of return by saving abroad. Bulow and Rogoff conjecture that, even under condition (ii), in more general reputation models with multiple relationships and spillover across them, reputation may support debt. This paper shows what is needed for this conjecture to be true.

The views expressed herein are those of the authors and not necessarily those of the Federal Reserve Bank of Minneapolis or the Federal Reserve System.

1. INTRODUCTION

The standard reputation argument for why sovereign governments repay debts is that governments fear that if they default, their tarnished reputations will spill over to future debt relationships and make bankers less willing to lend to them. (See, for example, Eaton and Gersovitz 1981; Kletzer 1984; Manuelli 1986; Grossman and Van Huyck 1988; Atkeson 1991; and Cole, Dow, and English 1995.) Bulow and Rogoff (1989b) challenge this traditional explanation. In a provocative paper, they show that “under fairly general conditions, lending to small countries must be supported by the direct sanctions available to creditors, and cannot be supported by a country’s ‘reputation for repayment’” (1989b, p. 43). A key reason for the difference between this result and the results in the rest of the literature is that Bulow and Rogoff assume that regardless of its past behavior, a government can earn the market rate of return on its savings by saving with foreign bankers (possibly with full sets of state-contingent contracts and state-contingent payoffs).¹ The rest of the literature, either explicitly or implicitly, assumes that if a country defaults, it cannot save.

Bulow and Rogoff go on to conjecture that reputation models of debt are not necessarily dead. More precisely, Bulow and Rogoff conjecture that since countries are involved in a myriad of relationships, reputation may be able to support debt even with their assumption if the analysis is expanded from the partial reputation models that view debt in isolation to a general reputation model that includes all the country’s relationships. In this paper, we examine the Bulow-Rogoff conjecture in a model in which misbehavior in the debt arena tarnishes a government’s reputation in other arenas. We find that whether or not the conjecture holds depends critically on the nature of the other relationship: if it is a repeated relationship, with constant per-period benefits, it may hold; if it is a dynamic relationship, with benefits that depend on the values of state variables, it may not.

Bulow and Rogoff prove their result in a model with complete information, an infinite horizon, uncertainty, and a single debt relationship. To set up our later analysis, we begin by reviewing how their result extends to a model with incomplete information, a finite horizon, no

exogenous uncertainty, and a single debt relationship. Abstracting from exogenous uncertainty is of no consequence; it simply makes the notation less cumbersome. Of more importance is our focus on incomplete information. We allow a small amount of uncertainty about whether the government attaches a large disutility to not honoring its contracts. (For some related work in industrial organization using reputation models with incomplete information, see Kreps and Wilson 1982 or Milgrom and Roberts 1982. For some related work in international economics, see Eaton 1992.²) Our result is in the spirit of Bulow and Rogoff: with a single debt relationship, reputation can support effectively zero debt.

We then turn to the main analysis and expand our partial reputation model, in which the debt relationship is modeled in isolation, to a general reputation model which includes all of a country's relationships. We capture this expanded view by adding to the simple model one other relationship. In this analysis, we focus on another relationship which has constant per-period benefits. We call it a *domestic labor relationship*, but it can be interpreted in many other ways. We find that even if there is a vanishingly small amount of uncertainty about the type of the government, the unique equilibrium of our model has reputation supporting as much debt as there would be under full commitment. That is, we show that there are circumstances under which a general reputation can support large amounts of positive debt.

The main contribution of this paper is to investigate Bulow and Rogoff's conjecture about the ability of reputation to support debt. The results here clarify the circumstances under which their conjecture holds. For it to hold, two conditions must be satisfied. First, misbehavior in the debt relationship must spill over to another relationship. For this condition to hold requires only a trivial amount of uncertainty in the minds of the lenders and the workers about whether the government might honor its contracts for some reason other than the readily observable costs and benefits it faces. Second, the payoffs in the other relationship must yield net benefits from maintaining a good reputation which are, in some sense, both large enough and persistent enough. In general, for these

net benefits to be calculated, the whole equilibrium must be calculated, and simple conditions cannot be put on the primitives of the environment to ensure that the resulting spillover is enough to support large amounts of debt. In the special, but common, setup in which the other relationship is a simple repeated one, these net benefits are constant, and simple conditions on the primitives of the environment can be calculated which ensure that large amounts of debt can be supported by spillover.

A secondary contribution of our paper is to exposit a model of a country's general reputation which is potentially interesting in its own right. Indeed, if the Bulow and Rogoff (1989b) paper is viewed as having killed the standard reputation models (and having laid the groundwork for the subsequent direct-sanctions approach adopted by Bulow and Rogoff 1989a, Fernandez and Rosenthal 1990, and others), then this paper can be viewed as reviving the reputation approach.

2. AN ECONOMY WITH ONE TRUST RELATIONSHIP

We begin with an incomplete-information economy that consists of two countries and lasts a finite number of periods. One country has a number of risk-neutral bankers. The other country is represented by the government, which has access to a country-specific investment project and needs to borrow resources to fund it. There are two types of government: a normal government and an honest government. A *normal* government is risk-neutral and discounts the future at rate β . An *honest* government has the same utility as the normal one except that it experiences a large disutility from breaking contracts. The type of the government is private information. Bankers hold subjective beliefs about what type the government is, and they update these beliefs after seeing the actions of the government. We will show that in this economy, reputation can support effectively zero debt. To show this, we set up and define a Bayesian equilibrium. We show that as the bankers' prior belief that the government is honest shrinks to zero in an appropriate fashion, the associated equilibrium converges to one with zero debt.

Specifically, in each period t , $t = 0, \dots, T$, the economy has a perishable consumption-capital good. Bankers are risk-neutral, live for one period, have a discount factor β , and are endowed with

a large amount of the consumption-capital good in each period. Without loss of generality, we suppose that each period has two bankers, who are denoted $i = 1, 2$. The normal government has these preferences:

$$(1) \quad \sum_{t=0}^T \beta^t c_t,$$

where c_t is the government's consumption in period t . The honest government has these same preferences except that if it fails to honor a contract it has signed, its utility is the expression in (1) minus a large positive constant M . In each period t , an investment of x_t units in period t produces output of $A_t x_t$ units in period $t + 1$. Here A_t is a deterministically fluctuating productivity parameter that specifies the investment project's gross return. For simplicity, we assume that

$$(2) \quad A_t = \begin{cases} A, & \text{if } t \text{ is odd} \\ 0, & \text{if } t \text{ is even} \end{cases}.$$

(Letting productivity fluctuate is an easy way to give the government an incentive to borrow. This simple pattern of fluctuations makes the resulting borrowing pattern simple, but is otherwise inessential.) The project has a maximal size of 1 in the sense that $x_t \leq 1$. Throughout the paper, we will assume that the discount factor satisfies this condition:

$$(3) \quad \beta A > 1$$

as well as $\beta < 1$. The government is endowed with $x_0 = 0$ units of the consumption-capital good at the beginning of period 0.

A precise description of the timing of events in the model is as follows. In each period t , the government starts with new output, $A_t x_t$, and the value of debt either owed or saved, $R_t b_t$, where R_t is the gross interest rate and b_t is the amount borrowed by the government at $t - 1$. The government decides whether to repay old loans subject to this constraint:

$$(4) \quad z_t R_t b_t \leq A_t x_t,$$

where $z_t = 1$ corresponds to repayment by the government and $z_t = 0$, to default. Each banker $i = 1, 2$, having seen the default decision as well as the past actions of all agents, first offers the government a gross interest rate R_{t+1}^i . Then, after bankers have seen each other's interest rate offers, they each offer a loan size b_{t+1}^i . (By allowing bankers to condition their loan sizes on their competitor's interest rate offer, we avoid the possible nonexistence of equilibrium with pure strategies for lenders, as discussed in a related context by Jaffee and Russell 1976.) A loan contract s_{t+1} is a pair (R_{t+1}, b_{t+1}) that specifies a gross interest rate and a loan amount. Let S_{t+1} denote the set of loan contracts offered. The government is thus offered loan contracts s_{t+1}^i by bankers $i = 1, 2$, and so $S_{t+1} = (s_{t+1}^1, s_{t+1}^2)$. Faced with such a set of contracts, the government chooses a contract and randomizes if there are ties. The government also chooses how much to consume, c_t , and invest, x_{t+1} , subject to a constraint on the maximal size of the project,

$$(5) \quad x_t \leq 1,$$

and on the government's budget,

$$(6) \quad c_t + x_{t+1} - b_{t+1} = A_t x_t - z_t R_t b_t.$$

To build intuition, let us begin by examining an economy in which institutions are such that agents in both countries can commit to repaying their loans. Competition between bankers ensures that in each period t , the equilibrium gross rate of interest on loans is $R_t = \rho$, where $\rho \equiv 1/\beta$. From (3), we know that the return on the project, A , is greater than ρ ; hence, with such an interest rate in each even-numbered period, the government optimally borrows to fully fund the project. Thus, in each even-numbered period, starting with period 0, the government borrows 1, invests it, and consumes 0. In the next odd-numbered period, the project yields A units of output, out of which the government repays the banker ρ , consumes the rest $A - \rho$, and borrows 0. The discounted value of utility under commitment is, thus,

$$(7) \quad (A-\rho) + \beta^2(A-\rho) + \beta^4(A-\rho) + \dots = \frac{A - \rho}{1 - \beta^2}.$$

Of course, given that the government has linear preferences and that the discount factor of the government β satisfies $\beta = 1/\rho$, the timing of consumption by the government can be structured in a variety of ways to yield the same discounted value of utility.

Consider now the environment without such commitment. We set up and define equilibrium as follows. The *history* $h_t = \{[z_0, S_1, s_1, x_1, c_0], \dots, [z_{t-1}, S_t, s_t, x_t, c_{t-1}]\}$ records past actions of the government and the bankers up to period t . A *strategy for the government* at t is a probability of repaying $\sigma_t^i(h_t)$, $i = n, h$ (normal or honest), at the beginning of the period together with loan contract, investment, and consumption decisions denoted $s_{t+1}(h_t, z_t, S_{t+1})$, $x_{t+1}(h_t, z_t, S_{t+1})$, and $c_t(h_t, z_t, S_{t+1})$ made after both the realization of repayment decision z_t and the offer of the new set of loan contracts S_{t+1} . A *strategy for each banker* $i = 1, 2$ at t is an interest rate $R_{t+1}^i(h_t, z_t)$ and a loan size $b_{t+1}^i(h_t, z_t, R_{t+1})$, where $R_{t+1} = (R_{t+1}^1, R_{t+1}^2)$. We let $S_{t+1}(h_t, z_t, R_{t+1})$ denote the set of such contracts. Bankers also have a set of common *beliefs*, or priors, $p_t(h_t)$ that gives the probability of the government being honest conditional on the history.

A *perfect Bayesian equilibrium* is a set of strategies for the normal and honest governments and a set of strategies and beliefs for the bankers that satisfy the following conditions: (i) For each history, given the strategies and beliefs of the bankers from t onward and given the strategies of the governments from $t + 1$ onward, the strategies of the governments at t maximize the governments' payoffs among the set of strategies that satisfy (4)–(6) and $s_{t+1}^i(h_t, z_t, S_{t+1}) \in S_{t+1}(h_t, z_t, R_{t+1})$ for $i = n, h$. (ii) For each history, given the strategies of the governments, the strategy of the other banker at t , and the beliefs of banker j , the strategy of banker j maximizes this banker's payoffs for $j = 1, 2$. (iii) Bankers' beliefs are updated according to Bayes' rule.

Notice that in the above setup, bankers are not allowed to default. One interpretation of this assumption is that bankers have a commitment device that commits them to honoring all contracts they sign. It will be clear that in any equilibrium, regardless of the government's past actions, if the government wants to save any amount (any $b_{t+1} < 0$), then the bankers will oblige them and,

moreover, competition among bankers will drive the interest rate on such savings up to $R_{t+1} = \rho$. We will sometimes refer to these bankers as *Swiss bankers* in order to emphasize the feature that they are willing to let any government save with them regardless of the government's reputation.

We have shown in previous work (Cole and Kehoe 1995) that the level of borrowing in this economy is effectively zero. To do so, we used a standard (but complicated) backward induction argument to compute the equilibrium for this economy. We showed that if the initial prior and the initial capital were small enough, then the equilibrium value of utility and the initial borrowing level were both close to 0. To make this sense of closeness precise, we considered a sequence of economies in which the prior shrank to zero as the horizon length converged to infinity. More precisely, we proved this proposition:

PROPOSITION 1. Consider a sequence of economies indexed by the horizon length T , with $\beta < 1$, in which the initial prior $p_0(T)$ converges to 0 as T converges to infinity. Along this sequence, the equilibrium discounted value of utility converges to 0, and the initial borrowing converges to 0.

3. AN ECONOMY WITH MULTIPLE TRUST RELATIONSHIPS

In this section, we add to the model of Section 2 other relationships that involve trust. For another relationship to help support debt, we need misbehavior in the debt relationship to spill over and tarnish the government's reputation in the added relationship. It turns out that a small amount of incomplete information similar to that in Section 2 will generate such spillover in equilibrium. We also need the net benefits of maintaining a good reputation to be both large and persistent. We illustrate these conditions by means of some very simple examples. It will be clear that more elaborate examples can be constructed along the same lines.

Clearly, the most trivial way to add another trust relationship to the model above is to add another debt relationship with another group of bankers in another country which simply replicates the first. Let's do that. Let the information setup be the same as before except that the honest

government suffers a loss in utility if it breaks contracts with either group of bankers. In any Bayesian equilibrium of the model, the honest government will honor all contracts with both groups if the utility cost of breaking them is sufficiently large. Thus, if either group of bankers sees a government break either type of contract, the bankers will know for sure that the government is not honest. A simple backward induction argument implies that bankers will never lend to a government they know is not honest. Hence, the normal government will either honor both contracts or break both, since breaking either causes the government to lose its reputation. Thus, reputation from the trust involved in one debt relationship spills over to the trust involved in the other and vice versa.

A moment's reflection should make it clear that even though there is spillover across the debt relationships, only the same level of effectively zero debt that could be supported with the single debt relationship can be supported here. Since both the benefits and the costs of defaulting in the model with two projects are simply twice what they are in the model with one project, the default decisions are unchanged. Hence, even with spillover from one debt relationship to another, no more debt can be supported than could be before.

While this exercise is useful, it is somewhat special because the added relationship is totally symmetric to the existing one. We need to see that even if misbehavior in the debt relationship spills over to a very different type of relationship, this spillover may not support debt. For example, in Cole and Kehoe (1994), we show that spillover to a relationship involving exhaustible resources may not support debt. However, if the other relationship is the typical repeated relationship studied in almost all of the game theory literature, then the results may be different. We illustrate this point by considering a simple repeated labor relationship in which the per-period benefits are constant.

Consider adding a labor relationship to the debt model. This labor relationship emanates from a project that is available in each period. If the number of workers hired at the beginning of the period is N_t , then the project's output that same period is AN_t . The project has a maximal size of N in the sense that $N_t \leq N$. (The assumption that the labor project has the same productivity as the

debt project in odd-numbered periods is for notational simplicity only.) The economy has a large number of workers who have the specialized skills the government needs to run the project. Each of these workers is risk-neutral and has an alternative employment opportunity that earns a worker ω units with certainty in each period. We assume that

$$(8) \quad \beta A \geq \omega.$$

We will model the government as maximizing its utility, subject to its resource constraints. With a little more notation, we could reinterpret the model as one in which the government maximizes the welfare of its citizens, provides public goods by using specialized resources, and taxes in a distorting way.

For the sake of intuition, note that under commitment, the allocations are as follows. In period 0, the government borrows and invests 1, hires N workers, and consumes 0. In period 1, the investment and labor projects yield a total of $A + AN$ units of output, out of which the government pays the bankers ρ and pays the workers ωN . The government borrows and invests 0 and consumes $(A - \rho) + (A - \omega)N$. In period 2 and any even-numbered period after that, the labor project yields AN , out of which the government pays the workers ωN and consumes $(A - \omega)N$. The government also borrows 1 and invests it. Here, as in Section 2 with linear preferences and $\beta = 1/\rho$, the timing of consumption by the government can be structured in a variety of ways to yield the same discounted value of utility.

Now consider the model without commitment. The timing of the model is the same as before, with these additions. In the beginning of each period, each of the large number of workers offers an employment schedule. Each worker i offers to supply $n_t(i, w_t)$ units of labor to the government for a promise of w_t units of pay, where n_t is either 0 or 1. Confronted with a continuum of such wage schedules, all of which are identical, the government announces some particular wage w_t together with an employment cap N_t . The output of the project is realized immediately. After that, the government decides whether or not to honor its contracts with the bankers and the workers. We let $z_t^b = 1$ and

$z_t^n = 1$ correspond to honoring the debt and labor contracts. The constraints faced by the government are

$$(9) \quad z_t^b R_t b_t + z_t^n w_t N_t \leq A_t x_t + AN_t$$

together with

$$(10) \quad c_t + x_{t+1} - b_{t+1} = A_t x_t + AN_t - z_t^b R_t b_t - z_t^n w_t N_t$$

and

$$(11) \quad x_{t+1} \leq 1 \text{ and } N_t \leq N.$$

In (10), we have assumed that the number of workers is N_t .

The specification of the governments is similar to that before. There are two types of government: a normal government and an honest government. A *normal* government is risk-neutral and discounts the future at rate β . An *honest* government evaluates consumption streams the same way as the normal government, but an honest government also assigns a large disutility to breaking any contract it has signed, that is, either the debt contract or the labor contract. In particular, we can write the preferences of an honest government as

$$(12) \quad \sum_{t=0}^T \beta^t [c_t - (1-z_t^b)M^b - (1-z_t^n)M^n],$$

where M^b and M^n are large positive numbers. (Recall that $z_t^b = 1$ and $z_t^n = 1$ correspond to honoring the debt and labor contracts and $z_t^b = 0$ and $z_t^n = 0$ correspond to defaulting on these contracts.) The type of the government is private information. Both bankers and workers hold subjective beliefs about what type the government is, and they update these beliefs after seeing the actions of the government.

The same logic we used above with two debt relationships should make clear here that in any Bayesian equilibrium of this model, the honest government will honor all debt and labor contracts if M^b and M^n are sufficiently large, which we will henceforth assume to be true. Thus, if a private agent, either a banker or a worker, sees the government default on either type of contract, the agent

will know for sure that the government is not honest. A simple backward induction argument implies that workers will never work for, or bankers lend to, a government that they know is not honest. Hence, the normal government will either honor both contracts or default on both, since defaulting on either one causes the government to lose its reputation. Thus, the reputation from the trust involved in the debt relationship necessarily spills over to the trust involved in the labor relationship and vice versa.

One way to analyze the model's implications for government borrowing is to compute the equilibrium directly by backward induction. However, a more convenient way is to develop some simple properties of the equilibrium indirectly. To do that, we first backtrack a little: we consider a model that has only a labor project and develop in that model an expression for the value of reputation in the labor relationship alone. We then consider the model with both the debt and labor relationships. We use the result that losing trust in the debt relationship spills over to the labor relationship to show how the full commitment level of debt can be supported.

Consider the model in which we set $x_t = b_t = 0$ for all t . The formal definition of a Bayesian equilibrium is similar to the one in the previous section; here we proceed more informally. In the Bayesian equilibrium that we consider, the workers' beliefs about the government are summarized by a conditional probability that the government is honest. We denote this conditional probability at t by p_t and call it the *reputation* of the government. In this equilibrium, the history of past events at the beginning of period t is summarized by the conditional probability p_t . The strategies of agents are allowed to depend on p_t together with the actions that have already occurred within the period. Thus, the work decision of worker i can be written as $n_t(i, w_t, p_t)$. The model's interesting equilibria turn out to involve the government randomizing, or *mixing*, over whether or not to honor its contract. Let σ_t^n denote the probability that the normal government honors the contract. The equilibrium we compute has two requirements: At every possible state, each agent acts optimally, given the strategies and beliefs of other agents, and beliefs are updated according to Bayes' rule wherever possible. Since

the honest government never defaults on contracts ($\sigma_t^h \equiv 1$), Bayes' rule implies that the probability that the government is honest at $t + 1$, conditional on honoring its contract at t (and all previous periods), is

$$(13) \quad p_{t+1} = \frac{p_t}{p_t + (1-p_t)\sigma_t^n}.$$

In each period t , each of the N workers will supply one unit of labor if the expected wage is greater than or equal to ω . If the honest government always honors contracts and the normal government honors them with probability σ_t , then at an offered wage of

$$(14) \quad w_t = \frac{\omega}{p_t + (1-p_t)\sigma_t^n},$$

the workers will receive an expected wage of ω . Hiring workers will only be profitable for the honest government if the wage rate is less than the return on the project, that is, if

$$(15) \quad w_t \leq A.$$

Backward induction works in this model exactly as it does in the standard Kreps-Wilson (1982) and Milgrom-Roberts (1982) models of the chain store paradox. Solving backward to period 0 gives the following value function:

$$(16) \quad V_0(p_0, T) = \left\{ \begin{array}{ll} \sum_{s=0}^{T-1} \beta^s (A-\omega)N + \beta^T AN & \text{if } \omega/A \leq p_0 \leq 1 \\ \sum_{s=0}^{T-2} \beta^s (A-\omega)N + \beta^{T-1} AN & \text{if } (\omega/A)^2 \leq p_0 < \omega/A \\ \vdots & \vdots \\ (A-\omega)N + \beta AN & \text{if } (\omega/A)^T \leq p_0 < (\omega/A)^{T-1} \\ AN & \text{if } (\omega/A)^{T+1} \leq p_0 < (\omega/A)^T \\ 0 & \text{if } p_0 < (\omega/A)^{T+1} \end{array} \right\}.$$

This value function corresponds to the following equilibrium behavior. In the lowest region, defined by $p_0 < (\omega/A)^{T+1}$, no mixing probability is both high enough to give a wage $w_0 < A$ and low enough to push up next period's prior into the next-highest region. Hence, workers do not work at period

0. Workers do not revise their priors, and then $p_1 = p_0$, and workers do not work at period 1, and so on. The value of utility is, thus, zero. In the next-highest region, with $(\omega/A)^{T+1} \leq p_0 < (\omega/A)^T$, workers work, and the government is just indifferent between currently defaulting on its contract and honoring it. Thus, the value of utility is AN . In the next-highest region, with $(\omega/A)^T \leq p_0 < (\omega/A)^{T-1}$, the government strictly prefers to honor its contract this period and start mixing the next period. Thus, today it gets $(A-\omega)N$ units of consumption; from tomorrow on, the value of its utility is AN ; and its total utility is $(A-\omega)N + \beta AN$. For the next-highest region, the government strictly prefers to honor the contract for two periods and then start mixing, which gives it a total utility of $(A-\omega)N + \beta(A-\omega)N + \beta^2 AN$, and so on.

Consider now the equilibrium behavior for a fixed prior p_0 as the time horizon lengthens. Suppose k is an integer such that

$$(17) \quad (\omega/A)^{k+1} \leq p_0 < (\omega/A)^k.$$

Then the government honors its contracts for sure in the first $T - k$ periods. In periods $T - k + 1$ through $T - 1$, it will mix, and in period T , it will default. As T gets longer, so does the length of time that the government honors its contracts for sure, and in the limit, the government never defaults.

This equilibrium has a feature that we will use later. Given any initial prior $p_0 > 0$, let $k(p_0)$ be the integer such that (17) holds. Thus, in period $T - k(p_0)$, the government is just indifferent between defaulting on and honoring its contracts, and the value of either is AN . One period earlier, at $T - k(p_0) - 1$, the value of honoring is $(A-\omega)N + \beta AN$, or

$$(18) \quad AN + (\beta A - \omega)N.$$

By assumption, $\beta A > 1 > \omega$, so that as we move back one period, the value of honoring contracts strictly increases while the value of defaulting remains fixed at AN . Thus, there is a strictly positive gap of $(\beta A - \omega)N$ between these values. Continuing in this manner, we see from (16) that j periods before $T - k(p_0)$ the value of honoring contracts can be rewritten as

$$(19) \quad AN + \frac{(1-\beta)^j}{1-\beta} (\beta A - \omega)N,$$

while the value of defaulting is simply AN . Thus, the gap between the value of honoring and the value of defaulting monotonically increases as we move back in time from $T - k(p_0)$.

We will construct borrowing, investing, and repaying allocations which coincide with the full commitment levels for all but a fixed, finite number of periods at the end of the game. Given some k' , let these allocations specify that the government follow the full commitment allocations before $T - k'$ and at $T - k'$ switch to self-financing the investment project. More precisely, given some k' chosen such that $T - k'$ is odd for $t = T - k'$, let these allocations specify that out of total output $A + AN$, the government repay bankers ρ and pay workers ωN . Now, instead of borrowing 0 and consuming the rest, the government saves $1/\rho$ and consumes the rest. In period $T - k' + 1$ and each even-numbered period thereafter, the government receives AN from the labor project and 1 from the savings. The government invests 1, hires N workers, and consumes $(A - \omega)N$. In period $T - k' + 2$ and each odd-numbered period thereafter, the government receives a total output of $A + AN$, repays bankers 0, pays workers ωN , saves $1/\rho$, and consumes the rest, namely, $(A - 1/\rho) + (A - \omega N)$.

For what k' can these allocations be supported in the reputation model with both a debt project and a labor project? To compute this number, ignore spillover for a moment, and consider only the direct costs and benefits of defaulting on the debt contract with the bankers. In any period $t \leq T - k'$, the net benefits of defaulting on the debt contract are simply the saving of funds used to repay the loan, namely, ρ . For $t > T - k'$, there are no loans, so the net benefits of defaulting are zero. Now add back in the spillover effects. For some given prior p_0 , if we set $k' = k(p_0) + 1$, the difference between the value of honoring both debt and labor contracts and defaulting on them in period $T - k'$ is $(\beta A - \omega)N - \rho$. In any odd-numbered period before this, the net benefits of defaulting on the debt contract are the same, namely, ρ , while the gap between honoring and defaulting on the labor contract increases. In any even-numbered period, there is no debt and thus no benefit to defaulting. In any later period, there is no debt, so the net benefits of defaulting on it are obviously zero. Thus, if

$$(20) \quad \rho < (\beta A - \omega)N,$$

then it is possible to support the full commitment allocations from period 0 through period $T - k'$ with $k' = k(p_0) + 1$. More generally, for any given β , let $j(\beta)$ be the first integer such that the net benefits of defaulting on the debt contract are smaller than the net gains from paying the workers; namely,

$$(21) \quad \rho < \frac{(1-\beta^j)}{1-\beta} (\beta A - \omega)N.$$

If $T - [k(p_0) + j(\beta)]$ is odd, let $k' = k(p_0) + j(\beta)$, and otherwise, let $k' = k(p_0) + j(\beta) - 1$. Then, using the same reasoning as before, we can support the full commitment allocations up to period $T - k'$.

Next consider the strategies in this equilibrium. For computational reasons, we have found it convenient to express these strategies as functions of the state variable p_t . Of course, the more general way of defining strategies in game theory is to define them as functions of the entire history of past actions of the players. It is obvious that for $t < T - k'$, the strategies of the normal government, the bankers, and the workers are such that if the government has never defaulted on either contract, the lenders and workers continue with their full commitment actions, while if it has defaulted, bankers do not lend and workers do not work. (Of course, for $t \geq T - k'$, these strategies are somewhat more complicated.) We summarize our discussion with

PROPOSITION 2. *There exists a $\underline{\beta} \in (0,1)$ such that for all $\beta \in (\underline{\beta},1)$, the equilibrium allocations coincide with those under full commitment from period 0 through period $T - k'$, where $k' = k(p_0) + j(\underline{\beta})$.*

There is a precise sense in which the allocations in the economy with multiple trust relationships converge to the full commitment allocations even though the amount of uncertainty about the type of government becomes arbitrarily small. To understand that precise sense, consider the following:

Condition. The sequence of priors, $p(T)$, satisfies

$$(22) \quad (\rho/A)^{k(T)+1} \leq p_0(T) < (\rho/A)^{k(T)},$$

where $k(T)$ converges monotonically to infinity as T does and $T - k(T)$ converges to infinity.

Since $\rho/A < 1$, clearly $p_0(T)$ monotonically converges to zero as T converges to infinity. Now consider a sequence of economies indexed by T and $p_0(T)$. Along such a sequence, the importance of the honest government is monotonically declining to zero. Notice that in a sense, the prior is shrinking to zero more slowly than the horizon length is growing to infinity.

Now consider a sequence of economies indexed by T and $p_0(T)$, where $p_0(T)$ satisfies the above condition. Let $\underline{\beta}$ be such that (21) is satisfied for some finite $j(\underline{\beta})$. Using (16) and the above analysis, we can show straightforwardly that the equilibrium value of utility converges to the full commitment level.

4. INTERPRETATION AND EXTENSIONS

As we mentioned in the introduction, one contribution of this paper is to investigate the conditions under which the Bulow and Rogoff (1989b) result holds. The results of Section 3 clarify when it will hold and when it won't. Another contribution of the paper is to expost a model of the general reputation of countries which may be interesting in its own right. With this in mind, let's discuss the plausibility of the assumptions.

Our main results depend on there being some reputation spillover across different arenas of behavior. We obtained these results by assuming a small amount of uncertainty about whether the government is an honest type. But how should this assumption be interpreted? We adopt an interpretation in the spirit of that given by Kreps and Wilson (1982) and Milgrom and Roberts (1982) in the chain store paradox literature. In a chain store game, in order for a monopolist to deter the entry of incumbents, these researchers allow a small probability that there is an irrational monopolist who fights any entrant. In their work, all of the interesting theorems are proven as limits as the

probability of this irrational type goes to zero and the number of periods of the game goes to infinity. The interpretation these researchers give for their assumption is that there really is no irrational type; rather, this setup captures a vanishingly small uncertainty in the minds of the potential entrants that they may be facing a monopolist who plays tough. The normal monopolist understands that incumbents have this trivial amount of doubt, and it is exploited to build the monopolist a reputation. Indeed, Selten (1978) and Milgrom and Roberts (1982) think that the case of absolutely zero uncertainty in the minds of players (including uncertainty about other players possibly being uncertain) is unrealistic and, moreover, that this case generates predictions inconsistent with plausible behavior.

We interpret our uncertainty assumption in the same way. We think of the uncertainty about government honesty as being in the minds of agents who are in trust relationships with a country about the motives of the government for behaving well in any relationship. As long as the agents are not completely certain that there are no potential adverse consequences to the government in another relationship (or, at least, as long as this fact is not common knowledge to all other such agents), an equilibrium like ours should exist.

At an intuitive level, the basic idea here is that if someone is thought to be sleazy or untrustworthy in one relationship, the person will be thought of as likely to be sleazy or untrustworthy in other relationships. At this level, the idea applies to everything from business relationships to dating relationships—to just about any relationships that involve trust. Applied to relationships among nations, this idea seems quite plausible.

In terms of extensions of our work, recall that we interpret the model as having Swiss bankers who allow any agent to save with them, regardless of the agent's reputation. Imagine that in this model, we added Swiss bankers who would sign and honor any contract for which they were both paid up front and given the market rate of return. In such a model, imagine trying to break the equilibrium we considered with the following deviation. In the first period, the workers work for the

government and the government defaults on the labor contract. The government then gives the goods to a Swiss banker, with instructions to pay ω to any worker who works for the government the next period. This type of deviation continues for all future periods. If this deviation were both feasible and profitable, it would break our equilibrium.

There are several ways to amend the model so that such a deviation does not work. The simplest is to assume that, after a Swiss banker pays the wages to the domestic worker, the government can confiscate them. Clearly, then, the original equilibrium would remain. Another way to amend the model is to add some private information known to the private agents and the government. Suppose the government is involved with a large number of possibly very heterogeneous types of domestic agents who each can provide some valuable work effort. Then, even if the hours of each and every agent are publicly observable, if the effort and the quality of output are the private information of the private agents and the government, then the Swiss banker would not be able to duplicate the government's payment schedule. The inefficiency of having the Swiss banker administer the contracts could be used to construct a reputation equilibrium similar to the one considered here. Yet another way to amend the model is to let the maximal size of the labor project grow. If the rate of growth of the project were sufficiently high, then the contemplated deviation would not be profitable. This growing labor project might capture the idea that in a developing economy, the size and value of the government's relationships involving trust are continually expanding.

Finally, note that there are clearly other types of uncertainty about the types of government which would not generate reputation spillover. It should be obvious, however, that regardless of what other types of government exist, as long as at least one type attaches a large disutility to breaking both contracts, reputation will still support lending. Indeed, the equilibrium of the model then is similar to the analysis here.

We have examined the Bulow and Rogoff (1989b) conjecture that since actual economies are involved in a myriad of relationships, general reputation models with potential spillover across relationships may be able to support good outcomes. We have found that in a class of models, this conjecture does not hold if reputation spills over to other relationships with only transient benefits, but it does hold if reputation spills over to a relationship with enduring benefits.

The idea that an agent's reputation in one relationship may spill over to other relationships is certainly not new. However, in most of the literature, the spillover is such that actions of agents in one arena of behavior affect reputation in that arena only. In the debt literature, for example, if a government defaults on a loan, it ruins its reputation in the debt arena; in the industrial organization literature on entry deterrence, if an incumbent doesn't fight entry, it ruins the incumbent's reputation in the entry-deterrence arena. Here we have shown that when the spillover stays within the debt arena, reputation cannot support lending. For reputation to support lending, a government's actions in the debt arena must spill over to a different arena, such as labor relationships. Viewed this way, the benefits of maintaining a good relationship in one arena cannot be calculated simply by looking at that arena alone. Instead, account must be taken of the ramifications in a variety of other arenas, which, at least on the surface, may not seem to be directly connected to the original arena, where misbehavior might occur.

This basic idea can be applied in many contexts. It might explain why countries honor some commitments, like treaties, when a narrow cost/benefit analysis would recommend breaking them. Consider, for example, a fishing treaty between the United States and Canada. Suppose that at the time the treaty was signed, it seemed like a good idea, but later developments revealed that the treaty was costing the United States a lot. Nonetheless, the United States might honor the treaty because breaking it would damage its reputation with Canada in other arenas that involve trust. Moreover, breaking that treaty might cause a negative reputation spillover to, say, Japan in a completely different arena that involves a trust relationship, such as a mutual defense pact.

Notes

¹Others have looked at other conditions for the existence of a reputation equilibrium. Pesendorfer (1992) considers a scenario in which the government must assemble an optimal portfolio from existing financial assets in the world market. Pesendorfer shows that even if the set of world assets is complete, adding the restriction that each asset in the portfolio must be held in a positive position may force the government to bear risk. The fear of bearing such risk may be sufficient to give the government an incentive to repay its debt. Mohr (1991) shows that a reputation equilibrium might exist in an overlapping generations model if a government can run a type of rational Ponzi scheme.

²Eaton (1992), following Diamond (1989), considers a reputation model which has two types of borrowers: “good” borrowers, for whom the lender can costlessly destroy output if they default, and “normal” borrowers, for whom the lender cannot do that. Eaton, however, assumes that there is no way to save after a default, so his model does not satisfy the Bulow and Rogoff (1989b) assumption on the ability to save.

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